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# BINARY SEARCH TREES

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Problem Solving with Computers-I

<https://ucsb-cs24-sp17.github.io/>



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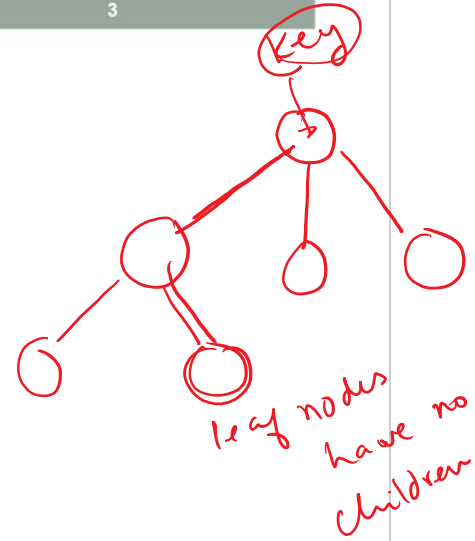
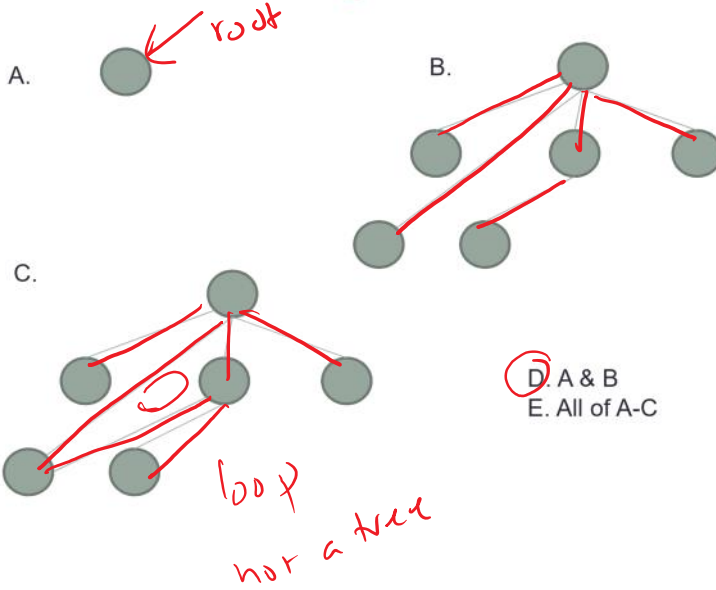
## Imposter panel: Tomorrow Thurs (06/01), 12:30pm to 1:50pm, HFH 1132



Come hear faculty, grad students and undergrad alumni talk about their careers and how they dealt with feeling like an Imposter!

Please RSVP : <https://goo.gl/forms/ttvzHNPWAZ0GCPA92>

Which of the following is/are a tree?



# Lab08: Binary Search Tree – What is it?

data record that can contain other fields → keys, any datatype that allows comparison

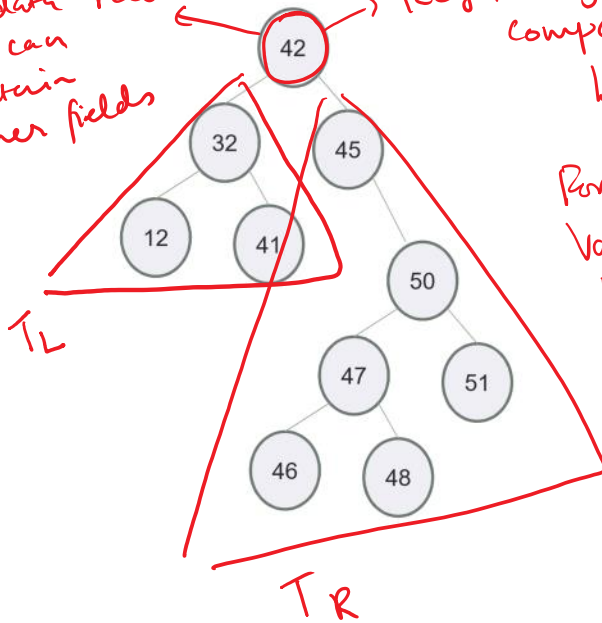
key: ← ordering is available on the keys

For any node in a BST  
value of all nodes in the left subtree  $\leq$  value of the node

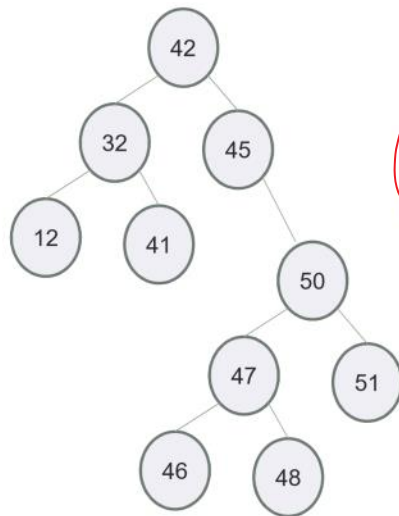
$T_L \leq$  value of node

value of node  $<$   $T_R$

What are the numbers in the nodes?

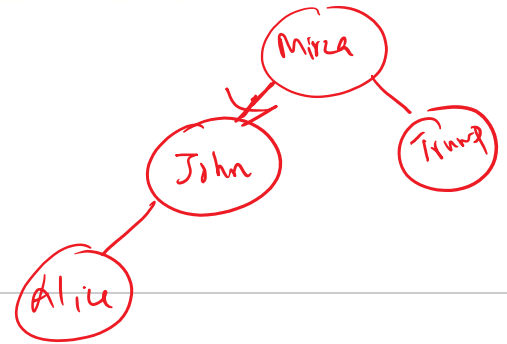


## Binary Search Tree – What is it?

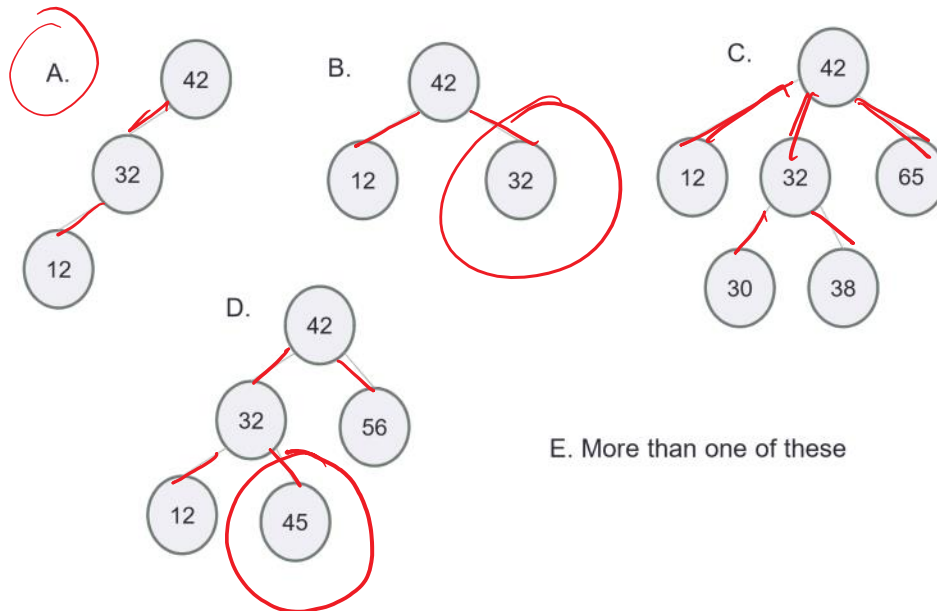


For any node,  
Keys in node's left subtree  $\leq$  Node key  
Node key  $<$  Keys in node's right subtree

Do the keys have to be integers?



Which of the following is/are a binary search tree?



E. More than one of these

## Binary Search Trees

• What are the operations supported?

↓  
search, insert, delete, min, max,  
next, largest (successor)  
next, smallest (predecessor)

• What are the running times of these operations?

(log N)

• How do you implement the BST i.e. operations supported by it?

## Binary Search Trees

- What is it good for?
  - If it satisfies a special property i.e. Balanced, you can think of it as a dynamic version of the sorted array

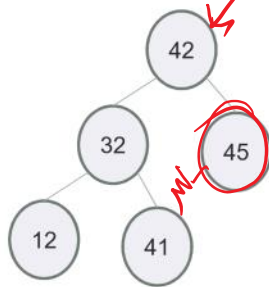
everything that is supported by a  
sorted array + Fast insert  
& delete  
~  
↓  
(under some  
condition)



## Under the hood: Searching an element in the BST

To search for element with key  $k$

1. Start at the root
2. If  $k = \text{key}(\text{root})$ , found key, stop.
3. Else If  $k < \text{key}(\text{root})$ , recursively search the left subtree:  $T_L$   
Else recursively search the right subtree:  $T_R$

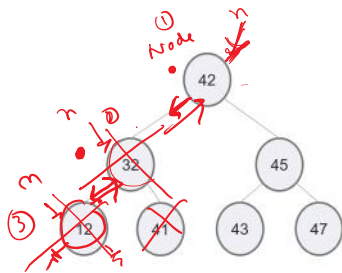


Search for 41.  
Now search for 43.

# Traversing the BST

Different methods of tree traversal:

- ~~In order traversal~~
- Pre order traversal
- Post order traversal



```

struct Node {
  int data;
  Node * left;
  Node * right;
  Node * parent;
}

```

```

void inorder ( Node *n ) {
  if ( n == 0 )
    return;
  inorder ( n->left );
  cout << n->data << " ";
  inorder ( n->right );
}

```

```

void preorder ( Node *n ) {
  if ( n ) {
    cout << n->data << " ";
    preorder ( n->left );
    preorder ( n->right );
  }
}

```

12 32 41 42 43 45 47

$O(N)$

BST, with templates:

```
template<typename Data>

class BSTNode {
public:
    BSTNode<Data>* left;
    BSTNode<Data>* right;
    BSTNode<Data>* parent;
    Data const data;

    BSTNode( const Data & d ) :
        data(d) {
        left = right = parent = 0;
    }
};
```

BST, with templates:

```
template<typename Data>
```

```
class BSTNode {  
public:  
    BSTNode<Data>* left;  
    BSTNode<Data>* right;  
    BSTNode<Data>* parent;  
    Data const data;  
  
    BSTNode( const Data & d ) :  
        data(d) {  
            left = right = parent = 0;  
        }  
};
```

How would you create a **BSTNode** object on the runtime stack?

- A. `BSTNode n(10);`
- B. `BSTNode<int> n;`
- C. `BSTNode<int> n(10);`
- D. `BSTNode<int> n = new BSTNode<int>(10);`
- E. More than one of these will work

{ } syntax OK too

BST, with templates:

```
template<typename Data>
```

```
class BSTNode {  
public:  
    BSTNode<Data>* left;  
    BSTNode<Data>* right;  
    BSTNode<Data>* parent;  
    Data const data;  
  
    BSTNode( const Data & d ) :  
        data(d) {  
        left = right = parent = 0;  
    }  
};
```

How would you create a **pointer** to BSTNode with integer data?

- A. BSTNode\* nodePtr;
- B. BSTNode<int> nodePtr;
- C. BSTNode<int>\* nodePtr;

BST, with templates:

```
template<typename Data>
```

```
class BSTNode {  
public:  
    BSTNode<Data>* left;  
    BSTNode<Data>* right;  
    BSTNode<Data>* parent;  
    Data const data;
```

```
    BSTNode( const Data & d ) :  
        data(d) {  
        left = right = parent = 0;  
    }  
};
```

Complete the line of code to create a new BSTNode object with int data on the heap and assign nodePtr to point to it.

```
BSTNode<int>* nodePtr
```

## Working with a BST

```
template<typename Data>
class BST {

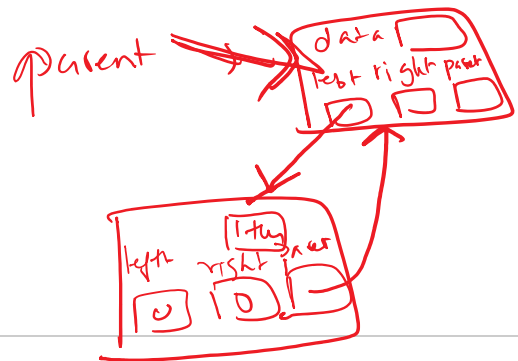
private:

    /** Pointer to the root of this BST, or 0 if the BST is empty */
    BSTNode<Data>* root;

public:

    /** Default constructor. Initialize an empty BST. */
    BST() : root(nullptr){ }

    void insertAsLeftChild(BSTNode<Data>* parent, const Data & item)
    {
        // Your code here
    }
}
```



## Working with a BST: Insert

```
void insertAsLeftChild(BSTNode<Data>* parent, const Data & item)
{
    // Your code here
}
```

Which line of code correctly inserts the data item into the BST as the left child of the parent parameter.

- A. `parent.left = item;`
- B. `parent->left = item;`
- C. `parent->left = BSTNode(item);`
- D. `parent->left = new BSTNode<Data>(item);`
- E. `parent->left = new Data(item);`

*parent → left → parent = parent;*

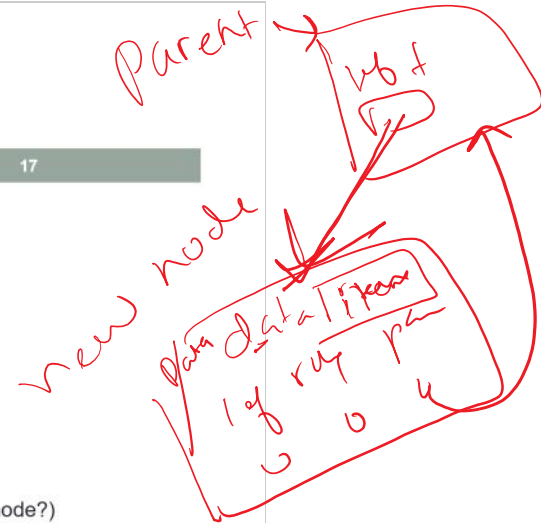


## Working with a BST: Insert

```
template <class Data>  
void insertAsLeftChild(BSTNode<Data>* parent, const Data & item)  
{  
    parent->left = new BSTNode<Data>(item);  
}
```

Is this function complete? (i.e. does it do everything it needs to correctly insert the node?)

- A. Yes. The function correctly inserts the data
- B. No. There is something missing.



## Working with a BST: Insert

```
void insertAsLeftChild(BSTNode<Data>* parent, const Data & item)
{
    parent->left = new BSTNode<Data>(item);
}
}
```